

4 Calculations Used in Analytical Chemistry

4A SOME IMPORTANT UNITS OF MEASUREMENT

4A-1 SI Units

SI Base Units

Physical Quantity	Name of unit	Abbreviation	International system of units (SI)
Mass	kilogram	kg	
Length	meter	m	
Time	second	s	
Temperature	kelvin	K	
Amount of substance	mole	mol	
Electric current	ampere	A	
Luminous intensity	candela	cd	

Prefixes for units

Prefix	Abbreviation	Multiplier	Prefix	Abbreviation	Multiplier
yotta-	Y	10^{24}	deci-	d	10^{-1}
zetta-	Z	10^{21}	centi-	c	10^{-2}
exa-	E	10^{18}	milli-	m	10^{-3}
peta-	P	10^{15}	micro-	μ	10^{-6}
tera-	T	10^{12}	nano-	n	10^{-9}
giga-	G	10^9	pico-	p	10^{-12}
mega-	M	10^6	femto-	f	10^{-15}
kilo-	k	10^3	atto-	a	10^{-18}
hecto-	h	10^2	zepto-	z	10^{-21}
deca-	da	10	yocto-	y	10^{-24}

angstrom (\AA) : non-SI unit of length = 0.1 nm = 10^{-10} m.

4A-2 The Distinction Between Mass and Weight

Mass: invariant measure of the amount of matter in an object

Weight: the force of gravitational attraction between that matter and earth

$$W = m \times g$$

W : weight of an object, m : mass,
 g : acceleration due to gravity

4A-3 The Mole

Avogadro's number (6.022×10^{23})

the molar mass of formaldehyde CH_2O

$$\begin{aligned}M_{\text{CH}_2\text{O}} &= \frac{1 \text{ mol C}}{\text{mol CH}_2\text{O}} \times \frac{12.0 \text{ g}}{\text{mol C}} + \frac{2 \text{ mol H}}{\text{mol CH}_2\text{O}} \times \frac{1.0 \text{ g}}{\text{mol H}} + \frac{1 \text{ mol O}}{\text{mol CH}_2\text{O}} \times \frac{16.0 \text{ g}}{\text{mol O}} \\ &= 30.0 \text{ g/mol CH}_2\text{O}\end{aligned}$$

the molar mass of glucose $\text{C}_6\text{H}_{12}\text{O}_6$

$$\begin{aligned}M_{\text{C}_6\text{H}_{12}\text{O}_6} &= \frac{6 \text{ mol C}}{\text{mol CH}_2\text{O}} \times \frac{12.0 \text{ g}}{\text{mol C}} + \frac{12 \text{ mol H}}{\text{mol CH}_2\text{O}} \times \frac{1.0 \text{ g}}{\text{mol H}} + \frac{6 \text{ mol O}}{\text{mol CH}_2\text{O}} \times \frac{16.0 \text{ g}}{\text{mol O}} \\ &= 180.0 \text{ g/mol C}_6\text{H}_{12}\text{O}_6\end{aligned}$$

* Millimole (mmol) = 10^{-3} mol

1 mfw = 10^{-3} fw

no. of moles of a species X (no. mol A): $n_X = \frac{m_X}{M_X}$

Ex. 4-1. How many moles and millimoles of benzoic acid ($M=122.1$ g/mol) are contained in 2.00 g of the pure acid?

amount g HBz = $2.00 \text{ g} \times (1 \text{ mol}/122.1 \text{ g}) = 0.0164 \text{ mol HBz}$

amount g HBz = $2.00 \text{ g} \times (1 \text{ mmol}/0.1221 \text{ g}) = 16.4 \text{ mmol HBz}$

Ex. 4-2. How many grams of Na^+ (22.99 g/mol) are contained in 25.00 g of Na_2SO_4 (142.0 g/mol)?

amount $\text{Na}_2\text{SO}_4 = 25.00 \text{ g} \times (1 \text{ mol}/142.0 \text{ g}) = 0.17606 \text{ mol}$

since 1 mol of Na_2SO_4 contains 2 mol of Na^+ ,

amount $\text{Na}^+ = 2 \times 0.17606 \text{ mol} = 0.35211 \text{ mol}$

mass $\text{Na}^+ = 0.35211 \text{ mol} \times 22.99 \text{ g/mol} = 8.10 \text{ g}$

4B SOLUTIONS AND THEIR CONCENTRATIONS

4B-1 Concentration of Solutions

Molar Concentration (C)

$$C_X = \frac{n_X}{V}, \text{ molarity} = M = \frac{\text{no. mol solute}}{\text{no. L solution}} = \frac{\text{no. mmol solute}}{\text{no. mL solution}}$$

Ex 4-3 Calculate the molar conc. of ethanol in an aqueous solution that contains 2.30 g of C₂H₅OH (46.07 g/mol) in 3.50 L of solution.

$$\begin{aligned} \text{no. mol} &= 2.30 \text{ g} \times (1 \text{ mol}/46.07 \text{ g}) = 0.04992 \text{ mol} \\ C_{\text{C}_2\text{H}_5\text{OH}} &= 0.04992 \text{ mol}/3.50 \text{ L} = 0.01426 \text{ mol/L} = 0.0143 \text{ M} \end{aligned}$$

Analytical Molarity: total number of moles of a solute in 1 L solution

(How a solution has been prepared?)

Ex: 1.0 M H₂SO₄ soln → dissolving 1.0 mol or 98 g H₂SO₄ in water and diluting to exactly 1.0 L.

Equilibrium or Species Molarity: the molar conc. of a particular species in a soln. **at equilibrium**

Formal Concentration (Formality, F): analytical concentration

Ex: 1.00 F NaOH or H₂SO₄ → equilibrium molar conc. = 0.00 M

Ex 4-4. Calculate the analytical and equilibrium molar conc. of the solute species in an aqueous solution that contains 285 mg of trichloroacetic acid (Cl₃CCOOH, 163.4 g/mol) in 10.0 mL (the acid is 73 % ionized in water).

$$\text{no. mol HA} = 285 \text{ mg} \times (1 \text{ g}/1000 \text{ mg}) \times (1 \text{ mol}/163.4 \text{ g}) = 1.744 \times 10^{-3} \text{ mol}$$

$$C_{\text{HA}} = \frac{1.744 \times 10^{-3} \text{ mol HA}}{10.0 \text{ mL}} \times \frac{1000 \text{ mL}}{1 \text{ L}} = 0.174 \frac{\text{mol HA}}{\text{L}} = 0.174 \text{ M}$$

HA	⇌	H ⁺	+	A ⁻	[HA] = 0.174 mol/L × 0.27
Initial 100%		0%		0%	= 0.047 mol/L = 0.047 M
平衡後 27%		73%		73%	

$$\begin{aligned} [\text{H}_3\text{O}^+] &= [\text{A}^-] = C_{\text{HA}} - [\text{HA}] \\ &= 0.174 - 0.047 = 0.127 \text{ M} \end{aligned}$$

Ex 4-5. Describe the preparation of 2.00 L of 0.108 M BaCl₂ from BaCl₂ · 2H₂O (244 g/mol).

$$2.00 \text{ L} \times 0.108 \text{ mol/L} = 0.216 \text{ mol BaCl}_2 \cdot 2\text{H}_2\text{O}$$

$$0.216 \text{ mol} \times 244 \text{ g/mol} = 52.8 \text{ g BaCl}_2 \cdot 2\text{H}_2\text{O}$$

Dissolve 52.8 g of BaCl₂ · 2H₂O in water and dilute to 2.00 L.

Ex 4-6. Describe the preparation of 500 mL of 0.074 M Cl⁻ from solid BaCl₂ · 2H₂O (244 g/mol).

$$\text{mass BaCl}_2 \cdot 2\text{H}_2\text{O} = \frac{0.0740 \text{ mol Cl}^-}{\text{L}} \times 0.500 \text{ L} \times \frac{1 \text{ mol BaCl}_2 \cdot 2\text{H}_2\text{O}}{2 \text{ mol Cl}^-}$$

$$\times \frac{244.3 \text{ g BaCl}_2 \cdot 2\text{H}_2\text{O}}{\text{mol BaCl}_2 \cdot 2\text{H}_2\text{O}} = 4.52 \text{ g BaCl}_2 \cdot 2\text{H}_2\text{O}$$

Dissolve 4.52 g of BaCl₂ · 2H₂O in water and dilute to 500 mL.

Percent Concentration (% , parts per hundred)

weight % (w/w) = $\frac{\text{weight solute}}{\text{weight solution}} \times 100\%$	37 % HCl (w/w) soln: 37 g HCl per 100 g soln. 70 % HNO ₃ (w/w) soln
Volume % (v/v) = $\frac{\text{volume solute}}{\text{volume solution}} \times 100\%$	5 % CH ₃ OH (v/v) soln: diluting 5.0mL CH ₃ OH with H ₂ O to 100mL.
weight/volume % (w/v) = $\frac{\text{weight solute, g}}{\text{volume solution, mL}} \times 100\%$	5 % AgNO ₃ (w/v) soln: dissolving 5 g AgNO ₃ in H ₂ O to 100 mL.

Parts Per Million and Parts Per Billion (ppm & ppb)

$$C_{\text{ppm}} = (\text{mass of solute} / \text{mass of soln}) \times 10^6 \text{ ppm} \quad 1 \text{ ppm} = 1 \text{ mg/L}$$

$$C_{\text{ppb}} = (\text{mass of solute} / \text{mass of soln}) \times 10^9 \text{ ppb} \quad 1 \text{ ppb} = 1 \text{ } \mu\text{g/L}$$

$$C_{\text{ppt}} = (\text{mass of solute} / \text{mass of soln}) \times 10^3 \text{ ppt}$$

Ex 4-7. What is the molarity of K⁺ in an aqueous solution that contains 63.3 ppm of K₃Fe(CN)₆ (329.2 g/mol).

$$C_{\text{K}^+} = 63.3 \text{ g} / 10^6 \text{ g} \times 10^3 \text{ g/L} \times (1 \text{ mol} / 329.2 \text{ g}) \times 3 = 5.77 \times 10^{-4} \text{ M}$$

Solution-Diluent Volume Ratios

1:4 : dilute one volume with three volumes.

p-Function or p-value

For chemical species X: $\text{pX} = -\log [\text{X}]$ $\text{pH} = -\log [\text{H}^+]$

Ex: 4-8. 2.00×10^{-3} M NaCl and 5.4×10^{-4} M HCl solution

$$\text{pH} = -\log [\text{H}^+] = -\log (5.4 \times 10^{-4}) = 3.27$$

$$\text{pNa} = -\log (2.00 \times 10^{-3}) = 2.699$$

$$\text{pCl} = -\log (2.00 \times 10^{-3} + 5.4 \times 10^{-4}) = -\log (2.54 \times 10^{-3}) = 2.595$$

Ex: 4-9. Calculate the molar conc. of Ag^+ in a solution that has a pAg of 6.372.

$$[\text{Ag}^+] = \text{antilog} (-6.372) = 4.25 \times 10^{-7}$$

4B-2 Density and Specific Gravity of Solutions

***Density:** mass per unit volume, kg/m^3 , or g/mm^3 . (kg/L or g/mL)

***Specific Gravity:** the ratio of the mass of a substance to the mass of an equal volume of water (4°C).

Ex. 4-10. Calculate the molar conc. of HNO_3 (63.0 g/mol) in a soln that has a specific gravity of 1.42 and is 70 % HNO_3 (w/w).

$$1.42 \text{ Kg/L} \times 10^3 \text{ g/Kg} \times 70\text{g}/100\text{g} = 994 \text{ g/L}$$
$$C_{\text{HNO}_3} = 994 \text{ g/L} \times (1 \text{ mol}/63.0 \text{ g}) = 15.8 \text{ mol/L} = 16 \text{ M}$$

Ex. 4-11. Describe the preparation of 100 mL of 6.0 M HCl from a conc. reagent that has a specific gravity of 1.18 and is 37 % (w/w) HCl (36.5 g/mol).

$$C_{\text{HCl}} = 1.18 \times 10^3 \text{ g/L} \times 37 \text{ g}/100 \text{ g} \times (1 \text{ mol}/36.5 \text{ g}) = 12.0 \text{ M}$$

$$\text{amount HCl} = 100 \text{ mL} \times (1 \text{ L}/1000 \text{ mL}) \times 6.0 \text{ mol/L} = 0.600 \text{ mol}$$

$$\text{vol conc. reagent} = 0.600 \text{ mol} \times (1 \text{ L}/12.0 \text{ mol}) = 0.0500 \text{ L}$$

Dilute 50 mL of the conc. reagent to 100 mL.

Specific Gravities of Commercial Concentrated Acids and Bases

Reagent	Concentration % (w/w)	Specific Gravity
Acetic acid, CH_3COOH	99.7	1.05
Ammonia, NH_4OH	29.0	0.90
Hydrochloric acid, HCl	37.2	1.19
Hydrofluoric acid, HF	49.5	1.15
Nitric acid, HNO_3	70.5	1.42
Perchloric acid, HClO_4	71.0	1.67
Phosphoric acid, H_3PO_4	86.0	1.71
Sulfuric acid, H_2SO_4	96.5	1.84

4C CHEMICAL STOICHIOMETRY

Stoichiometry: the mass relationships among reacting chemical species.

4C-1 Empirical Formulas and Molecular Formulas

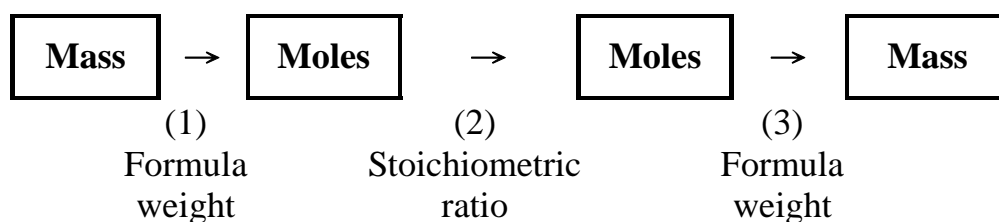
Empirical formula: the simplest whole-number ratio of atoms in a chemical compound.

Molecular formula: the number of atoms in a molecule.

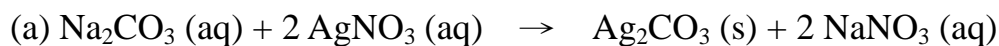
Structural formula:

	<i>Empirical formula</i>	<i>Molecular formula</i>	<i>Structural formula</i>
formaldehyde	CH ₂ O	CH ₂ O	HCHO
acetic acid	CH ₂ O	C ₂ H ₄ O ₂	CH ₃ COOH
glyceraldehyde	CH ₂ O	C ₃ H ₆ O ₃	
glucose	CH ₂ O	C ₆ H ₁₂ O ₆	
ethanol		C ₂ H ₆ O	C ₂ H ₅ OH
Dimethyl ether		C ₂ H ₆ O	CH ₃ OCH ₃

4C-2 Stoichiometric Calculations



Ex. 4-12. What Mass of AgNO₃ (169.9 g/mol) is needed to convert 2.33 g of Na₂CO₃ (106.0 g/mol) to Ag₂CO₃? (b) What mass of Ag₂CO₃ (275.7 g/mol) will be formed?



Step 1: $n_{\text{Na}_2\text{CO}_3} = 2.33 \text{ g} \times (1 \text{ mol}/106.0 \text{ g}) = 0.02198 \text{ mol}$

Step 2: $n_{\text{AgNO}_3} = 0.02198 \text{ mol} \times (2/1) = 0.04396 \text{ mol AgNO}_3$

Step 3: $m_{\text{AgNO}_3} = 0.04396 \text{ mol} \times 169.9 \text{ g/mol} = \mathbf{7.47 \text{ g AgNO}_3}$

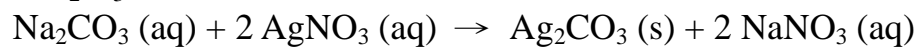
(b) $n_{\text{Ag}_2\text{CO}_3} = n_{\text{Na}_2\text{CO}_3} = 0.02198 \text{ mol}$

$m_{\text{Ag}_2\text{CO}_3} = 0.02198 \text{ mol} \times 275.7 \text{ g/mol} = \mathbf{6.06 \text{ g Ag}_2\text{CO}_3}$

Ex. 4-13. What mass of Ag_2CO_3 (275.7 g/mol) is formed when 25.0 mL of 0.200M AgNO_3 are mixed with 50.0 mL of 0.0800M Na_2CO_3 ?

$$n_{\text{AgNO}_3} = 25.0 \text{ mL} \times 0.200 \text{ M AgNO}_3 = 5.00 \text{ mmol AgNO}_3$$

$$n_{\text{Na}_2\text{CO}_3} = 50.0 \text{ mL} \times 0.0800 \text{ M Na}_2\text{CO}_3 = 4.00 \text{ mmol Na}_2\text{CO}_3$$



$$m_{\text{Ag}_2\text{CO}_3} = 5.00 \text{ mmol} \times 1/2 \times 0.2757 \text{ g /mmol} = 0.689 \text{ g Ag}_2\text{CO}_3$$

Ex. 4-14. What will be the molar analytical Na_2CO_3 conc. in the soln produced when 25.0 mL of 0.200 M AgNO_3 is mixed with 50.0 mL of 0.0800 M Na_2CO_3 ?

$$n_{\text{Na}_2\text{CO}_3} = 4.00 \text{ mmol} - (5.00 \text{ mmol} \times 1/2) = 1.50 \text{ mmol Na}_2\text{CO}_3$$

$$C_{\text{Na}_2\text{CO}_3} = 1.50 \text{ mmol} / (50.0 + 25.0) \text{ mL} = 0.0200 \text{ M Na}_2\text{CO}_3$$